# Understanding Self-Predictive RL

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# **Representation Learning**

Example: Visual tasks (Image classification, Segmentation, Depth estimation ...)

A classic problem, curse of dimensionality.

We need to embed the input into a low-dimensional space, but that causes information loss.

Then what information should we keep, and what should we discard?

Obviously, the ones necessary to solve our task!

**Representation Learning** = Learning to encode large inputs into smaller embeddings, while preserving the information required for the task(s).

## **Representation Learning**

End-to-end deep-learning is one form of representation learning.

e.g., CNN-encoder + MLP-predictor

Self-supervised / Unsupervised methods get representations useful for downstream tasks.

e.g., DINOv2





## Representation Learning for Reinforcement Learning

Similarly, representation learning is necessary in reinforcement learning as well.

Again, these could be learned by end-to-end deep learning,

e.g., Any model-free algorithm with deep networks (DQN, SAC, DDPG,  $\cdots$ )

or by self-supervised / unsupervised objectives.

e.g., Dreamer, TD-MPC, CURL, SPR, …

#### Introduction

Representation learning has become a hot topic in RL since around 2020. What should we choose, out of all these?



## Introduction

Representation learning has become a hot topic in RL since around 2020.

What if I told you that most of these boil down to latent self-prediction vs observation reconstruction?



## **Basic Notations**

Notation will be focused on POMDPs than MDPs.

MDP: Full access to the world/environment via state  $s_t$ .

POMDP: Partial access to the world/environment via observation  $o_t$ .

Unlike MDP, POMDP agents benefit from using history  $h_t = (h_{t-1}, a_{t-1}, o_t) = (o_1, a_1, o_2, a_2, \dots o_t)$ 

History Representations

Encoder  $\phi$ 

History representation  $z = \phi(h)$ 

# **Abstraction Theory**

"Abstraction can be thought of as a process that maps the ground representation, the original description of a problem, to an abstract representation, a much more compact and easier one to work with." (Li et al., 2006)

...so just embedding to a latent space.

Abstraction theory defines what kind of abstraction we want.

X-abstraction : The encoder provides an X-abstraction if it preserves all necessary information required for X.

Representation Learning =

Learning to encode large inputs into smaller embeddings, *while preserving the information required for the task(s).* 

[1] Towards a Unified Theory of State Abstraction for MDPs., Li et al., AlandM 2022.

Representation Learning =

Learning to encode large inputs into smaller embeddings, *while preserving the information required for the task(s).* 

What kind of information should be preserved in RL?

- 1. Information for predicting the return  $\rightarrow \phi_{Q^*}$  (Return prediction)
- 2. Information for predicting environment dynamics  $\rightarrow \phi_L$  (Latent self-prediction)
- 3. Information for predicting environment dynamics & observations  $\rightarrow \phi_0$  (Observation prediction)

- 1. Q\*-irrelevance abstraction ( $\phi_{Q^*}$ )
  - =  $\phi_{Q^*}$  preserves necessary information for predicting the true return Q<sup>\*</sup>.
  - = Formally,  $\phi_{Q^*}(h_i) = \phi_{Q^*}(h_j) \rightarrow Q^*(h_i, a) = Q^*(h_j, a), \forall a$

Learned by default in end-to-end model-free algorithms (DQN, SAC, ...)

Also learned by default in classic model-based algorithms (Dyna, Dreamer?)

- 2. Self-predictive abstraction / Model-irrelevance abstraction ( $\phi_L = RP + ZP$ )
  - =  $\phi_L$  preserves necessary information for predicting environment dynamics (reward + transition dynamics).
  - =  $\phi_L$  preserves necessary information for <u>expected reward prediction (RP)</u> AND for <u>next latent (z)</u> distribution prediction (ZP)

A weaker version of ZP is EZP – preserving information for expected next latent prediction (EZP)

$$\exists R_z : \mathcal{Z} \times \mathcal{A} \to \mathbb{R}, \quad s.t. \quad \mathbb{E}[r \mid h, a] = R_z(\phi_L(h), a), \quad \forall h, a,$$

$$\exists P_z : \mathcal{Z} \times \mathcal{A} \to \Delta(\mathcal{Z}), \quad s.t. \quad P(z' \mid h, a) = P_z(z' \mid \phi_L(h), a), \quad \forall h, a, z',$$

$$\mathbb{E}[z' \mid h, a] = \mathbb{E}[z' \mid \phi_L(h), a], \quad \forall h, a.$$

$$(EZP)$$

\*RP: There exists a function  $R_z$  capable of predicting the rewards from the representation  $\phi_L(h)$  = The representation have all information for reward prediction

- 3. Observation-predictive abstraction / Belief abstraction ( $\phi_0 = \text{RP} + \text{OP} + \text{Rec}$ )
  - =  $\phi_0$  preserves necessary information for predicting environment dynamics and its observations.
  - =  $\phi_0$  preserves necessary information for <u>expected reward prediction (RP)</u>

AND for <u>next observation (o) prediction (OP)</u>

AND is a <u>recurrent encoder (Rec)</u>

Rec condition is satisfied by regular feedforward or recurrent networks, *but not by Transformers*. (assume to be always satisfied)

Observation reconstruction (OR) is a condition closely related to OP.

$$\exists \psi_z : \mathcal{Z} \times \mathcal{A} \times \mathcal{O} \to \mathcal{Z}, \quad s.t. \quad \phi(h') = \psi_z(\phi_O(h), a, o'), \quad \forall h, a, o',$$
(Rec

$$\exists P_o: \mathcal{Z} \times \mathcal{A} \to \Delta(\mathcal{O}), \quad s.t. \quad P(o' \mid h, a) = P_o(o' \mid \phi_O(h), a), \quad \forall h, a, o', \tag{OP}$$

$$\exists \psi_o : \mathcal{Z} \to \mathcal{O}, \quad s.t. \quad o = \psi_o(\phi_O(h)), \quad \forall h.$$
 (OR)

[1] Approximate information state for approximate planning and reinforcement learning in partially observed systems., Subramanian et al., J. Mach. Learn. Res., 2022.

# Implication Graph

Authors prove that the conditions imply each other!

e.g., ZP + OR = OP (next latent prediction + obs reconstruction = next obs prediction)

In the same sense, abstractions also imply each other.

e.g.,  $\phi_0 = OP + RP + Rec = ZP + OR + RP + Rec = \phi_L + OR + Rec$ 





\*The source nodes of the edges with the same color together imply the target node.

## Back to Introduction

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Representation learning has become a hot topic in RL since around 2020.

What if I told you that most of these just end up learning either  $\phi_L$  or  $\phi_0$ ?

Work	PO?	Abstraction	Conditions	<b>ZP</b> loss	<b>ZP</b> target
Model-Free & Classic Model-Based RL	X	$\phi_{Q^*}$	$\phi_{Q^*}$	N/A	N/A
+VPN) MuZero (Schrittwieser et al., 2020)	×	unknown	$\phi_{Q^*} + \mathbf{RP}$	N/A	N/A
MICo (Castro et al., 2021)	×	unknown	$\phi_{Q^*}$ + metric	N/A	N/A
CRAR (François-Lavet et al., 2019)	×	$\phi_L$	$\phi_{Q^*} + \mathbf{RP} + \mathbf{ZP} + \mathrm{reg.}$	$\ell_2$	online
DeepMDP (Gelada et al., 2019)	×	$\phi_L$	$\phi_{Q^*} + \mathbf{RP} + \mathbf{ZP}$	$\mathrm{W}\left(\ell_{2} ight)$	online
SPR (Schwarzer et al., 2020)	×	$\phi_L$	$\phi_{Q^*}$ + ZP	COS	EMA
DBC (Zhang et al., 2020)	×	$\phi_L$	$\phi_{Q^*}$ + <b>RP</b> + <b>ZP</b> + metric	FKL	detached
LSFM (Lehnert & Littman, 2020)	×	$\phi_L$	$\phi_{Q^*}$ + RP + EZP	SF	detached
Baseline in (Tomar et al., 2021)	×	$\phi_L$	$\phi_{Q^*}$ + RP + ZP	$\ell_2$	detached
EfficientZero (Ye et al., 2021)	×	$\phi_L$	$\phi_{Q^*}$ + RP + ZP	COS	detached
TD-MPC (Hansen et al., 2022)	×	$\phi_L$	$\phi_{Q^*}$ + RP + ZP	$\ell_2$	EMA
ALM (Ghugare et al., 2022)	×	$\phi_L$	$\phi_{Q^*}$ + ZP	RKL	EMA
TCRL (Zhao et al., 2023)	×	$\phi_L$	RP + ZP	COS	EMA
OFENet (Ota et al., 2020)	X	$\phi_O$	$\phi_{Q^*}$ + OP	N/A	N/A
Recurrent Model-Free RL	<ul> <li>Image: A start of the start of</li></ul>	$\phi_{Q^*}$	$\phi_{Q^*}$	N/A	N/A
PBL (Guo et al., 2020)	✓	$\phi_L$	$\phi_{Q^*} + \mathbb{ZP}$	$\ell_2$	detached
AIS (Subramanian et al., 2022)	~	$\phi_L, \phi_O$	RP + ZP  or  OP	$\ell_2$ , FKL	detached
(PlaNet)Belief-Based Methods	~	$\phi_O$	RP + ZP + OR	FKL	online
Causal States (Zhang et al., 2019)	1	$\phi_O$	RP + OP	N/A	N/A
Minimalist $\phi_L$ (this work)	1	$\phi_L$	$\phi_{Q^*}$ + ZP	$\ell_2, \operatorname{KL}$	stop-grad



$$\phi_L = \mathsf{RP} + \mathsf{ZP}$$
  
$$\phi_O = \mathsf{RP} + \mathsf{OP} + \mathsf{Rec}$$

\* SAC-AE ( $\phi_0$ ) =  $\phi_{0^*}$  + OR

\* CURL (unknown) =  $\phi_{Q^*}$  + weak OR via contrastive loss

\* TD7 (unknown) = ZP

#### Minimalist Representation Learning

If all these methods end up with the same abstraction, why not use the most minimal condition set?

Work	PO?	Abstraction	Conditions	<b>ZP</b> loss	<b>ZP</b> target
Model-Free & Classic Model-Based RL	X	$\phi_{Q^*}$	$\phi_{Q^*}$	N/A	N/A
MuZero (Schrittwieser et al., 2020)	X	unknown	$\phi_{Q^*} + \mathbf{RP}$	N/A	N/A
MICo (Castro et al., 2021)	X	unknown	$\phi_{Q^*}$ + metric	N/A	N/A
CRAR (François-Lavet et al., 2019)	X	$\phi_L$	$\phi_{Q^*}$ + RP + ZP + reg.	$\ell_2$	online
DeepMDP (Gelada et al., 2019)	×	$\phi_L$	$\phi_{Q^*} + \text{RP} + \text{ZP}$	$\mathrm{W}\left(\ell_{2} ight)$	online
SPR (Schwarzer et al., 2020)	×	$\phi_L$	$\phi_{Q^*}$ + ZP	$\cos$	EMA
DBC (Zhang et al., 2020)	X	$\phi_L$	$\phi_{Q^*}$ + <b>RP</b> + <b>ZP</b> + metric	FKL	detached
LSFM (Lehnert & Littman, 2020)	×	$\phi_L$	$\phi_{Q^*}$ + RP + EZP	SF	detached
Baseline in (Tomar et al., 2021)	×	$\phi_L$	$\phi_{Q^*} + \operatorname{RP} + \operatorname{ZP}$	$\ell_2$	detached
EfficientZero (Ye et al., 2021)	×	$\phi_L$	$\phi_{Q^*} + \operatorname{RP} + \operatorname{ZP}$	cos	detached
TD-MPC (Hansen et al., 2022)	×	$\phi_L$	$\phi_{Q^*}$ + RP + ZP	$\ell_2$	EMA
ALM (Ghugare et al., 2022)	×	$\phi_L$	$\phi_{Q^*}$ + ZP	RKL	EMA
TCRL (Zhao et al., 2023)	×	$\phi_L$	RP + ZP	$\cos$	EMA
OFENet (Ota et al., 2020)	×	$\phi_O$	$\phi_{Q^*}$ + OP	N/A	N/A
Recurrent Model-Free RL	<ul> <li>Image: A start of the start of</li></ul>	$\phi_{Q^*}$	$\phi_{Q^*}$	 N/A	N/A
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AIS (Subramanian et al., 2022)	✓	$\phi_L, \phi_O$	RP + ZP  or  OP	$\ell_2$ , FKL	detached
Belief-Based Methods	✓	$\phi_O$	RP + ZP + OR	FKL	online
Causal States (Zhang et al., 2019)	-	$\phi_O$	RP + OP	N/A	N/A
Minimalist $\phi_L$ (this work)	1	$\phi_L$	$\phi_{Q^*} + \mathbb{ZP}$	$\ell_2, \mathrm{KL}$	stop-grad
Minimalist $\phi_0$	"	3.3	$\phi_{Q^*}$ + OP	"	3.3



 $\phi_L = \mathsf{RP} + \mathsf{ZP}$  $\phi_O = \mathsf{RP} + \mathsf{OP} + \mathsf{Rec}$ 

The self-predictive nature of latent prediction (ZP) poses a significant challenge.

The infamous representation collapse: ZP can be satisfied by mapping every input into a single latent. Mitigated by (1) Other losses like RP, or (2) Contrastive loss, or (3) Detaching the target encoder's gradient

Work	PO?	Abstraction	Conditions	<b>ZP</b> loss	<b>ZP</b> target
Model-Free & Classic Model-Based RL	X	$\phi_{Q^*}$	$\phi_{Q^*}$	N/A	N/A
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CRAR (François-Lavet et al., 2019)	×	$\phi_L$	$\phi_{Q^*}$ + <b>RP</b> + <b>ZP</b> + reg.	$\ell_2$	online
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LSFM (Lehnert & Littman, 2020)	X	$\phi_L$	$\phi_{Q^*} + \text{RP} + \text{EZP}$	SF	detached
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TCRL (Zhao et al., 2023)	X	$\phi_L$	RP + ZP	COS	EMA
OFENet (Ota et al., 2020)	X	$\phi_O$	$\phi_{Q^*}$ + OP	N/A	N/A
Recurrent Model-Free RL	-	$\phi_{Q^*}$	$\phi_{Q^*}$	N/A	N/A
PBL (Guo et al., 2020)	1	$\phi_L$	$\phi_{Q^*} + \mathbb{ZP}$	$\ell_2$	detached
AIS (Subramanian et al., 2022)	1	$\phi_L, \phi_O$	RP + ZP  or  OP	$\ell_2, FKL$	detached
Belief-Based Methods	1	$\phi_O$	RP + ZP + OR	FKL	online
Causal States (Zhang et al., 2019)	1	$\phi_O$	RP + OP	N/A	N/A
Minimalist $\phi_L$ (this work)	1	$\phi_L$	$\phi_{Q^*}$ + ZP	$\ell_2, \mathrm{KL}$	stop-grad



tl;dr

Theoretically, latent self-predictive losses are problematic in stochastic environments.

Theoretically, using stop gradient makes the problem less bad.

Authors will use stop-gradient from now on.

The self-predictive nature of latent prediction (ZP) poses a significant challenge.

The infamous representation collapse: ZP can be satisfied by mapping every input into a single latent.

Ideal ZP loss is unusable due to double sampling issue (i.e., cannot sample from the environment twice).

$$\mathcal{L}_{ZP,\mathbb{D}}(\phi,\theta;h,a) := \mathbb{E}_{z \sim \mathbb{P}_{\phi}(|h)}[\mathbb{D}(\mathbb{P}_{\theta}(z' \mid z, a) \mid \mid \mathbb{P}_{\phi}(z' \mid h, a))],$$
(1)

Instead, practical L2 or KL loss are used. However, these are theoretically okay only in deterministic MDPs.

$$J_{\ell}(\phi,\theta,\widetilde{\phi};h,a) := \mathbb{E}_{o' \sim P(|h,a)} \Big[ \|g_{\theta}(f_{\phi}(h),a) - f_{\widetilde{\phi}}(h')\|_{2}^{2} \Big],$$

$$\tag{2}$$

$$J_{D_{\mathbf{f}}}(\phi,\theta,\widetilde{\phi};h,a) := \mathbb{E}_{z \sim \mathbb{P}_{\phi}(|h),o' \sim P(|h,a)} \Big[ D_{\mathbf{f}} \left( \mathbb{P}_{\widetilde{\phi}}(z' \mid h') \mid \mid \mathbb{P}_{\theta}(z' \mid z,a) \right) \Big], \tag{3}$$

**Proposition 1** (The practical  $\ell_2$  objective Eq. 2 is an **upper bound** of the ideal objective Eq. 1  $\mathcal{L}_{ZP,\ell}(\phi,\theta;h,a)$  that targets EZP condition. The equality holds in deterministic environments.). **Proposition 2** (The practical f-divergence objective Eq. 3 is an **upper bound** of the ideal objective Eq. 1  $\mathcal{L}_{ZP,D_f}(\phi,\theta;h,a)$  that targets ZP condition. The equality holds in deterministic environments.).

Luckily, stop gradient operation mitigates the problem.

For L2 loss specifically, using stop gradient guarantees stationary point (online target doesn't). For linear models, stop gradient provably avoids representational collapse.



#### Minimalist $\phi_L$ Algorithm

 $\phi_{Q^*}$  + ZP (with L2 loss and stop-gradient)

Any Model-free algorithm + Auxiliary latent self-prediction loss

Algorithm 1 Minimalist  $\phi_L$ : learning self-predictive representations in RL

- **Require:** Encoder  $f_{\phi} : \mathcal{H}_t \to \mathcal{Z}$ , Actor  $\pi_{\nu} : \mathcal{Z} \to \mathcal{A}$ , Critic  $Q_{\omega} : \mathcal{Z} \times \mathcal{A} \to \mathbb{R}$ , Latent Transition Model  $g_{\theta} : \mathcal{Z} \times \mathcal{A} \to \mathcal{Z}$ . Learning Rate  $\alpha > 0$  and Loss Coefficient  $\lambda > 0$ .
- 1: **procedure** UPDATE(h, a, o', r)
- 2: Compute any model-free RL loss  $\mathcal{L}_{RL}$  (based on DDPG (Lillicrap et al., 2016) here) let  $Q^{\text{tar}}(h', r) := r + \gamma Q_{\overline{\omega}}(f_{\overline{\phi}}(h'), \pi_{\overline{\nu}}(f_{\overline{\phi}}(h'))),$

$$\mathcal{L}_{\mathrm{RL}}(\phi,\omega,\nu;h',r) = (Q_{\omega}(f_{\phi}(h),a) - Q^{\mathrm{tar}}(h',r))^2 - Q_{\overline{\omega}}(f_{\overline{\phi}}(h),\pi_{\nu}(f_{\phi}(h))).$$
(4)

- 3: Compute the auxiliary ZP loss  $\mathcal{L}_{aux}(\phi, \theta; h') = \|g_{\theta}(f_{\phi}(h), a) f_{\overline{\phi}}(h')\|_{2}^{2}$ .
- 4: Optimize all parameters using the sum of losses:

$$[\phi, \theta, \nu, \omega] \leftarrow [\phi, \theta, \nu, \omega] - \alpha \nabla (\mathcal{L}_{\mathsf{RL}}(\phi, \omega, \nu; h', r) + \lambda \mathcal{L}_{\mathsf{aux}}(\phi, \theta; h')).$$
(5)

#### Minimalist $\phi_L$ Algorithm

Enables comparing  $\phi_{Q^*}, \phi_L, \phi_O$  without changing the RL algorithm.

Set  $\lambda = 0 \rightarrow \phi_{Q^*}$ Change ZP to OP  $\rightarrow \phi_0$ 

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$$\mathcal{L}_{\mathrm{RL}}(\phi,\omega,\nu;h',r) = (Q_{\omega}(f_{\phi}(h),a) - Q^{\mathrm{tar}}(h',r))^2 - Q_{\overline{\omega}}(f_{\overline{\phi}}(h),\pi_{\nu}(f_{\phi}(h))).$$
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- 4: Optimize all parameters using the sum of losses:

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(5)

#### Does The Minimalist Algorithm Work?

Environment: Mujoco

Base algorithm: ALM(3)  $\rightarrow$  Mujoco SOTA

Minimalist  $\phi_L$  (ZP-L2, ZP-FKL, ZP-RKL) outperforms ALM(3) in all cases except Humanoid-v2. Both  $\phi_L$ ,  $\phi_O$  outperformed  $L_{Q^*}$  (TD3).



Figure 3: Decoupling representation learning from policy optimization using our algorithm based on ALM(3) (Ghugare et al., 2022). Comparison between  $\phi_{Q^*}$  (TD3),  $\phi_L$  (our algorithm (ZP- $\ell_2$ , ZP-FKL, ZP-RKL) and ALM(3)),  $\phi_O$  (OP- $\ell_2$ , OP-FKL), in the standard MuJoCo benchmark for 500k steps, averaged over 12 seeds. The observation dimension increases from left figure to right figure (17, 17, 111, 376).

# $\phi_L$ vs $\phi_O$

Hypothesis: Observation prediction ( $\phi_0$ ) is fragile to distractors. Environment: Distracting Mujoco (Gaussian noise) Base algorithm: ALM(3)  $\rightarrow$  Mujoco SOTA

 $\phi_L$  algorithms were more robust than  $\phi_O$  (OP-L2, OP-FKL).



Figure 5: Self-predictive representations are more robust. Comparison between  $\phi_{Q^*}$  (TD3),  $\phi_L$  (ZP- $\ell_2$ , ZP-FKL, ZP-RKL) using our algorithm,  $\phi_O$  (OP- $\ell_2$ , OP-FKL) in the distracting MuJoCo benchmark, varying the distractor dimension from  $2^4$  to  $2^8$ , averaged over 12 seeds. The y-axis is final performance at 1.5M steps.

# $\phi_L$ vs $\phi_O$

Hypothesis: Observation prediction  $(\phi_0)$  is fragile to distractors.

Environment: MiniGrid (POMDP + Sparse reward)

Base algorithm: R2D2 (Distributed RNN)

R2D2 + OP ( $\phi_0$ ) was more effective than R2D2 + ZP ( $\phi_L$ )



#### End-to-end vs Phased

Hypothesis: End-to-end learning (e.g., TD-MPC) and phased learning (e.g., Dreamer) won't matter Environment: MiniGrid (POMDP + Sparse reward)

Base algorithm: R2D2 (Distributed RNN)

End-to-end learning (OP, ZP) was way more effective than phased ones (RP+OP, RP+ZP)



#### Conclusion

Representation learning in RL boils down to latent self-prediction vs observation reconstruction.

End-to-end learning is just as effective as phased learning (TD-MPC vs Dreamer).

Choose either  $\phi_L$ ,  $\phi_O$  over  $\phi_{Q^*}$ .

 $\phi_L \ vs \ \phi_o$  depends on the task. Noisy/distracting tasks  $\rightarrow$  Try  $\phi_L$ Sparse-reward tasks  $\rightarrow$  Try  $\phi_o$